



筑波大学  
*University of Tsukuba*

# **Characterizing Reliability of Three-version Traffic Sign Classifier System through Diversity Metrics**

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# Outline

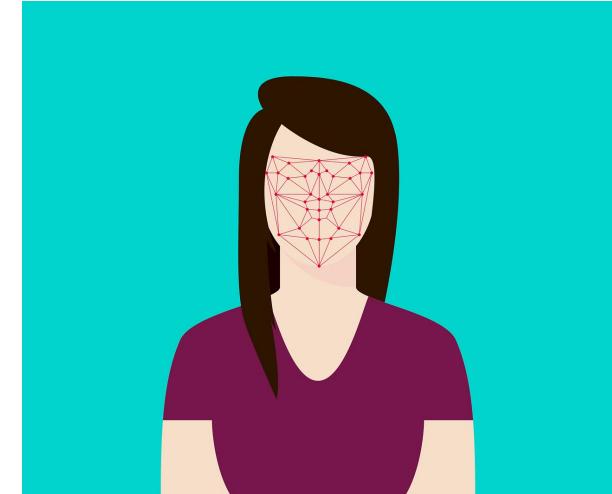
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1. Introduction
2. Related Work
3. Reliability Model
4. Objective
5. Experiment Configuration and Results
6. Conclusion & Future Work

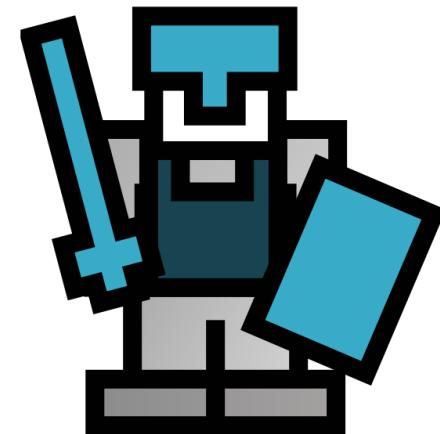
# 1. Introduction – Machine Learning Systems

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■ Machine learning (ML) models have been used in many intelligent software systems.



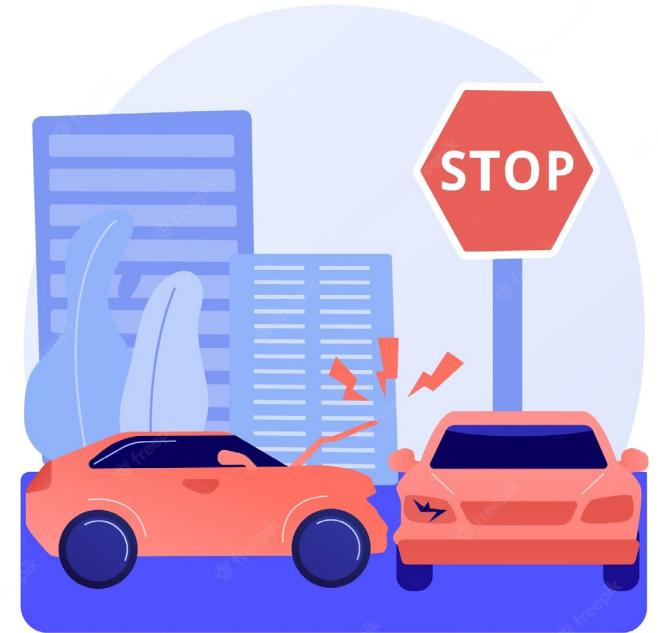
- Face recognition
- Medical diagnosis
- Autonomous robots and vehicles



# 1. Introduction – Reliability Issues of ML Systems

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- Outputs of ML models for real-world input data are not always correct
- Error outputs of ML models may induce undesirable consequences (e.g., traffic accidents in automated driving)



## 2. Related Work – Reliability Issues

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### ■ Approaches to ML system reliability improvement

- Data validations [1]

- Detect real-world error-inducing corner cases at runtime
- Require a white box model for deep neural networks

- Safety monitors [2]

- Detect out-of-distribution data at runtime
- Need to be trained together with the ML model in advance

- ✓ Redundant architecture [3-4]

- Achieve improved reliability by a simple redundancy scheme with diversity

## 2. Related Work – On Reliable ML Systems

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### ■ N-version ML system approach

- Multiple ML models [5]
- Diversified input data [7]

### ■ Issue of parameter estimation

- Estimation of diversity parameters
- The impacts of estimated diversity parameters on system reliability

## 2. Related Work – Diversity Measures

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### ■ Diversity Metrics

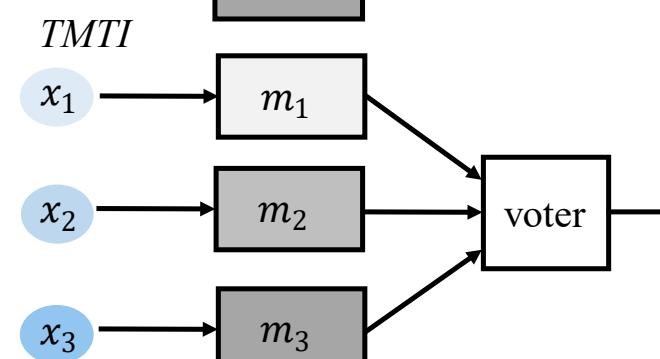
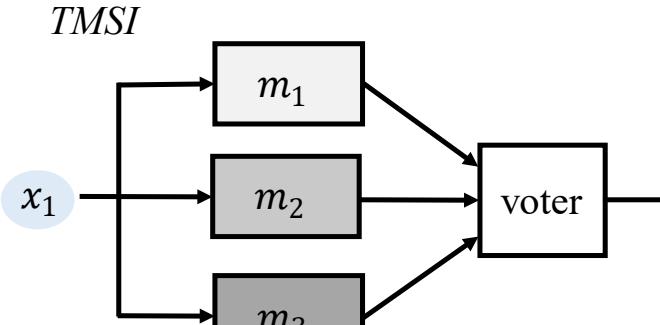
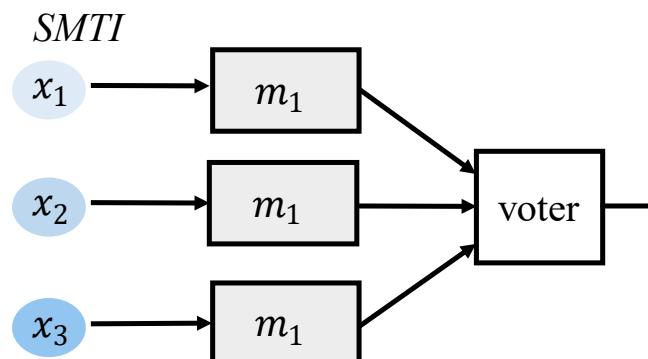
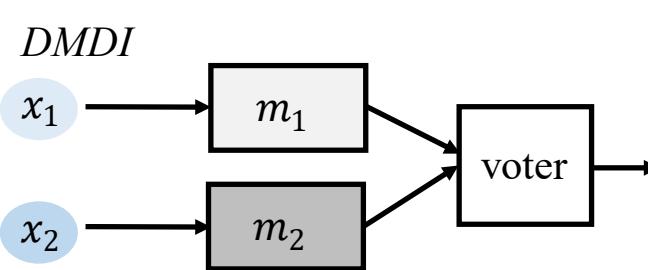
- Mutual error rate [6]
- Coverage of errors [7]
- Gini coefficient and the Shannon equitability index [8]

- The metrics are not applicable for diversity in different input data sources.
- The joint impact of model diversity and input diversity on system reliability is not discussed.

# 3. Reliability Model – N-version ML Architectures

## ■ Two-version and three-version ML architectures

- Double model with double input system (DMDI)
- Triple model with single input system (TMSI)
- Single model with triple input system (SMTI)
- Triple model with triple input system (TMTI)



### 3. Reliability Model – Conventional Reliability Model

- A conventional reliability model for a three-version system

$$R = 1 - [3\alpha f(1 - \alpha) + \alpha^2 f] = 1 - \alpha f(3 - 2\alpha)$$

- $R$ : Reliability of a three-version N-version Programming model
- $\alpha$ : A dependent failure parameter
- $f$ : The failure probability of each version

- Shortcomings

- The ratio of the dependence is **homogeneous** which may not be true in reality.
- The dependent failure parameter is **not enough** to represent the dependence of input data.

### 3. Reliability Model – Diversity Metrics [4]

■  $\alpha_{i,j}$  : Model diversity- Intersection of errors  $\alpha_{i,j} \in [0,1]$

- $E_i, E_j$  : The input sets that make ML models  $m_i$  and  $m_j$  output error
- A smaller intersection value is better-ML models are unlikely to reach a mutual error

$$\alpha_{i,j} = \frac{|E_i \cap E_j|}{\min\{|E_i, E_j|\}}$$

■  $\beta_{i,s|t}$  : Input diversity- Conjunction of errors  $\beta_{i,s|t} \in [0,1]$

- $x_s, x_t$ : Input data to ML models from different data sources (i.e.,  $s \neq t$ )
- A smaller conjunction value is better-the probability of a mutual error becomes small

$$\beta_{i,s|t} = \Pr[x_s \in E_i | x_t \in E_i]$$

### 3. Reliability Model – Reliabilities [4][9]

#### ■ Reliability of DMDI:

$$R_{2,2}(m_1, m_2; x_1, x_2) = 1 - \left[ \beta_{1,2|1} \cdot \alpha_{1,2} + (1 - \beta_{1,2|1}) \cdot \frac{p_2 - \alpha_{1,2} \cdot p_1}{(1 - p_1)} \right] \cdot p_1$$

#### ■ Reliability of TMSI:

$$\begin{aligned} R_{3,1}(m_1, m_2, m_3; x_1) \\ = 1 - (\alpha_{1,2} \cdot p_1 + \alpha_{1,3} \cdot p_1 + \alpha_{2,3} \cdot p_2 - 2\alpha_{1,2} \cdot \alpha_{1,3} \cdot p_1) \end{aligned}$$

#### ■ Reliability of SMTI:

$$R_{1,3}(m_1; x_1, x_2, x_3) = 1 - (\beta_{1,2|1} p_1 + \beta_{1,3|1} p_1 + \beta_{1,3|2} p_2' - 2\beta_{1,2|1} \beta_{1,3|1} p_1)$$

#### ■ Reliability of TMTI:

$$\begin{aligned} R_{3,3}(m_1, m_2, m_3; x_1, x_2, x_3) \\ = 1 - [p_{2,2}(m_1, m_2; x_1, x_2) + p_{2,2}(m_1, m_3; x_1, x_3) + p_{2,2}(m_2, m_3; x_2, x_3) - \\ 2p_{2,2}(m_1, m_2; x_1, x_2) \cdot p_{2,2}(m_1, m_3; x_1, x_3) / p_1] \end{aligned}$$

### 3. Reliability Model – Variants of Reliability Models

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#### ■ Five variants in the evaluation of TMSI reliability

$$R_{3,1}(m_1, m_2, m_3; x_1)$$

$$= 1 - (\alpha_{1,2} \cdot p_1 + \alpha_{1,3} \cdot p_1 + \alpha_{2,3} \cdot p_2 - 2\alpha_{1,2} \cdot \alpha_{1,3} \cdot p_1)$$

$$\begin{cases} t_1 = \alpha_{1,2} \cdot \alpha_{1,3} \cdot p_1 \\ t_2 = \alpha_{1,2} \cdot \alpha_{2,3} \cdot p_1 \\ t_3 = \alpha_{1,3} \cdot \alpha_{2,3} \cdot p_1 \\ t_4 = \frac{t_1 + t_2 + t_3}{3} \\ t_5 = \sqrt[3]{t_1 t_2 t_3} \end{cases}$$

# 4. Objective

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## ■ *Objective*

- Theoretical investigation of the reliability of N-version ML systems with model diversity and input diversity.
- Lack of discussion on the effectiveness of **diversity metrics** for reliability prediction.

## ■ *Empirical Experiment*

- Conduct experiments on **traffic sign recognition tasks** using deep neural networks
- Evaluate the reliability of **three-version traffic sign classifier architectures**
- Compare observed reliability with predicted reliability based on estimated diversity parameter values.

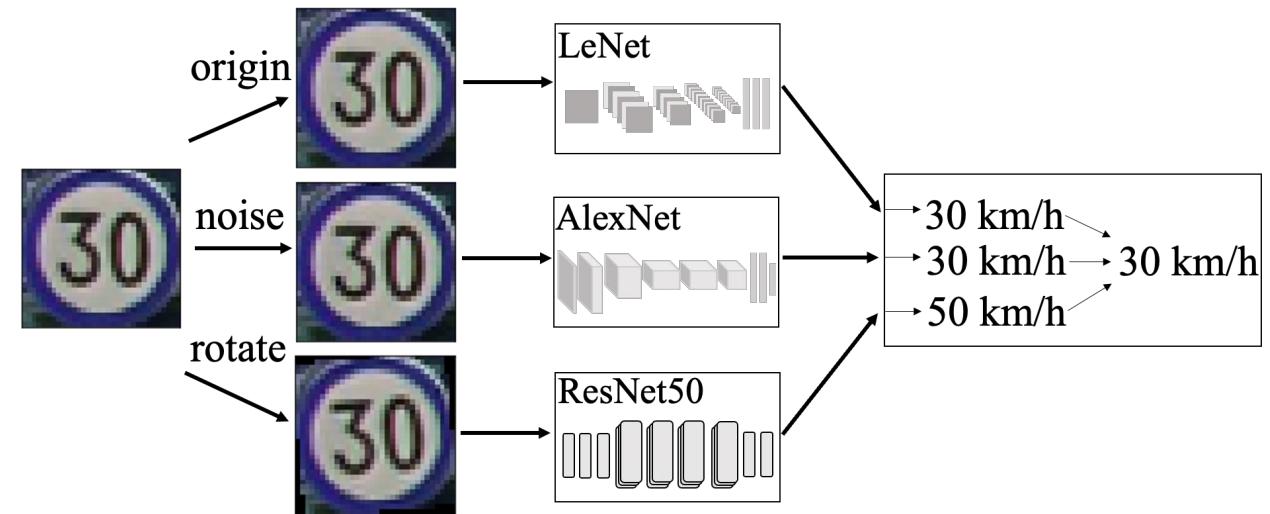
# 5. Experiment Configuration

## ■ *Model Diversity*

- LeNet
- AlexNet
- ResNet50

## ■ *Input Diversity*

- Original data
- Noise-added data
- Rotated data  
(rotate 5 degrees counterclockwise)



A three-version system by TMTI architecture

# 5. Experiment Configuration

## ■ *Datasets*

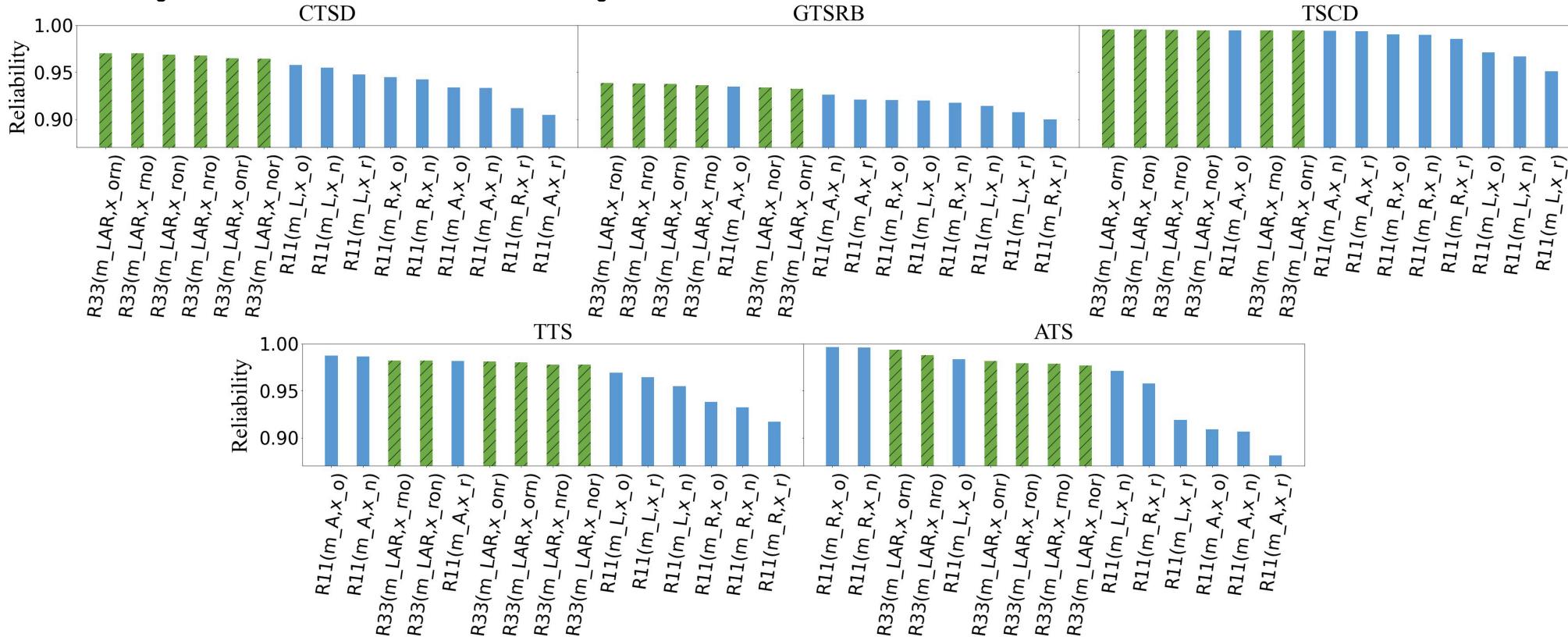
Five different traffic sign datasets

- Chinese Traffic Sign Dataset (CTSD)
- German Traffic Sign Recognition Benchmark (GTSRB)
- Traffic Sign Classification Dataset (TSCD)
- Turkey Traffic Sign (TTS)
- Arabic Traffic Signs (ATS)



# 5. Experiment Results – Research Question 1

◆ Does the implementation of a three-version system architecture effectively enhance reliability?

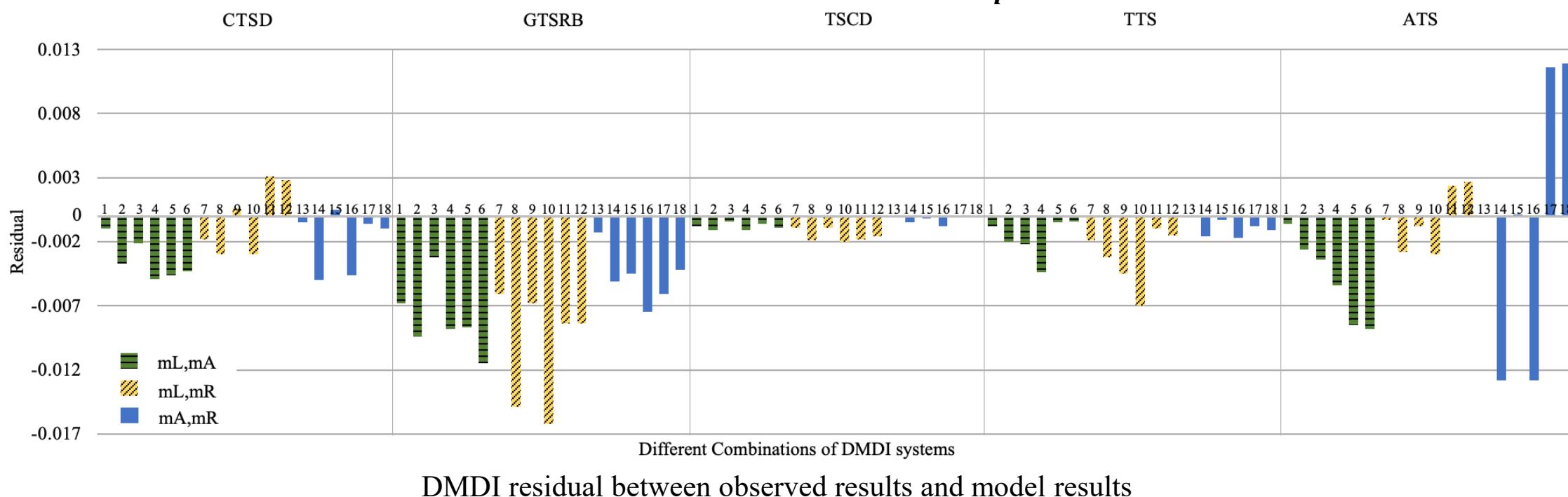


**Observation 1.** Three-version ML system architectures, especially the TMTI architecture, have the potential to efficiently improve system reliability compared to single models.

# 5. Experiment Results – Research Question 2

- ◆ How can the reliability models using diversity parameters estimate well the reliability of traffic sign classifier architectures?

- $e$  (Prediction residual) =  $R_{observed} - R_{predicted}$



**Observation 2.** The prediction residuals are mostly less than 0.017 across five data sets in most architectures except the SMTI architecture.

# 5. Experiment Results – Research Question 3

- ◆ How does the last term of the three-version reliability model impact on the reliability prediction?

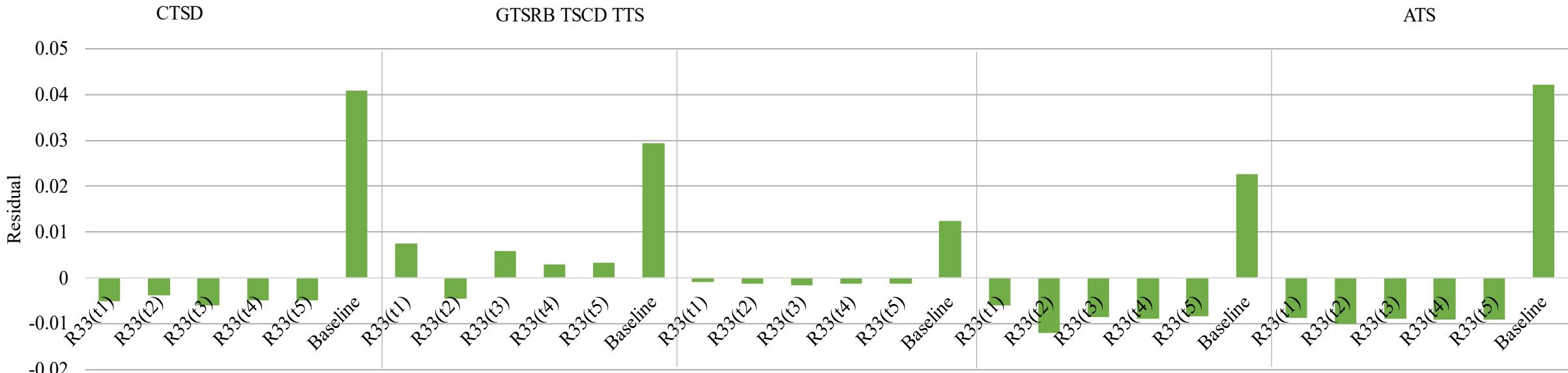
- Five variants in the evaluation of TMTI reliability

$$R_{3,3}(m_1, m_2, m_3; x_1, x_2, x_3) = 1 - [p_{2,2}(m_1, m_2; x_1, x_2) + p_{2,2}(m_1, m_3; x_1, x_3) + p_{2,2}(m_2, m_3; x_2, x_3) - 2p_{2,2}(m_1, m_2; x_1, x_2) \cdot p_{2,2}(m_1, m_3; x_1, x_3) / p_1]$$

$$\left\{ \begin{array}{l} t_1 = \frac{p_{2,2}(m_1, m_2; x_1, x_2) \cdot p_{2,2}(m_1, m_3; x_1, x_3)}{p_1} \\ t_2 = \frac{p_{2,2}(m_1, m_2; x_1, x_2) \cdot p_{2,2}(m_2, m_3; x_2, x_3)}{p_1} \\ t_3 = \frac{p_{2,2}(m_1, m_3; x_1, x_3) \cdot p_{2,2}(m_2, m_3; x_2, x_3)}{p_1} \\ t_4 = \frac{t_1 + t_2 + t_3}{3} \\ t_5 = \sqrt[3]{t_1 t_2 t_3} \end{array} \right.$$

# 5. Experiment Results – Research Question 3

## ■ Residual between observed results and model results for TMTI

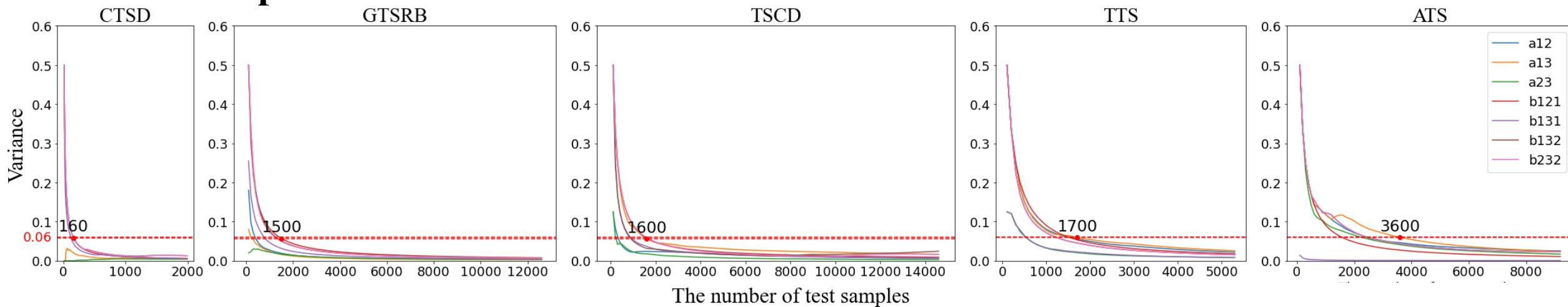


**Observation 3.** The residuals of five variants of TMSI, SMTI, and TMTI reliability predictions are equally effective. No variant shows evident superiority over the others.

# 5. Experiment Results – Research Question 4

- ◆ How many samples are required to obtain good estimates of the diversity parameter values?

- The trends of variances of estimated diversity parameters over the number of samples



**Observation 4.** For some data sets, we can obtain fairly good estimates of diversity parameters by a relatively small number of samples (less than a few thousand samples). In such cases, we may predict the reliability of three-version systems by measuring the diversities from early samples.

# 5. Experiment Results – Discussion

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## ■ Suggestions for reliable ML system design

- Adopt a three-version architecture, specifically emphasizing TMTI, for improved system reliability.
- Apply reliability models to select the most reliable three-version architecture based on observed diversities.
- For the architecture comparison purpose, a relatively small number of samples may be satisfactory for obtaining reasonable estimates of diversity parameters.

# 5. Experiment Results – Discussion

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## ■ Limitations

- Our observations are limited to traffic sign image recognition tasks.
- Decision schemes and voting rules for other tasks (e.g., object detection) require further investigation.
- Other system design factors, such as performance, resource consumption, energy, and cost need to be considered together with reliability.

# 6. Conclusion & Future Work

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## ■ Conclusion

- We investigate the reliability of N-version ML systems and the associated diversity metrics estimated from the empirical data.
- We focus on traffic sign recognition tasks and conduct experiments on five different traffic sign datasets.
- We answer five research questions and give suggestions for reliable ML system design.

## ■ Future work

- Explore other ML tasks
- Consider the cost and performance of N-version ML systems

# Reference

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Thank you for your attention!